

Assignment Sheet 6

Assignment 21 Fuzzy Relations

Let the fuzzy relation R be defined on the sets $X_1 = \{a, b, c\}$, $X_2 = \{s, t\}$, $X_3 = \{x, y\}$ and $X_4 = \{i, j\}$. Furthermore, let R be different than 0 at the following positions:

$$R(a, t, y, j) = 0.2,$$

$$R(b, s, x, j) = 0.5,$$

$$R(a, s, y, j) = 1.0,$$

$$R(a, s, y, i) = 0.9,$$

$$R(b, t, y, i) = 0.7,$$

$$R(c, s, y, j) = 0.3.$$

a) Compute the following projections of R :

$$R_{1,2,4} = [R \downarrow \{X_1, X_2, X_4\}],$$

$$R_{1,3} = [R \downarrow \{X_1, X_3\}],$$

$$R_4 = [R \downarrow \{X_4\}].$$

b) Compute the following cylindric extensions:

$$[R_{1,2,4} \uparrow \{X_3\}],$$

$$[R_{1,3} \uparrow \{X_2, X_4\}],$$

$$[R_4 \uparrow \{X_1, X_2, X_3\}].$$

Assignment 22 Fuzzy Relations

Prove that not every fuzzy relation R on $X \times Y$ is the Cartesian product of two fuzzy sets A of X and B of Y .

Assignment 23 Fuzzy Relations

Let R be a fuzzy relation on $X \times Y$ and S, T fuzzy relations on $Y \times Z$. Find an example where $R \circ (S \cap T) \subset (R \circ S) \cap (R \circ T)$ holds.

Assignment 24 Fuzzy Binary Relations

The fuzzy binary relation R is defined on set $X = \{1, 2, \dots, 100\}$ and $Y = \{50, 51, \dots, 100\}$ and represents the relation “ x is much smaller than y ”. It is defined by its membership function

$$R(x, y) = \begin{cases} 1 - \frac{x}{y}, & \text{if } x \leq y \\ 0, & \text{otherwise,} \end{cases}$$

whereas $x \in X$ and $y \in Y$.

Fuzzy Systems

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- a) What is the domain of R ?
- b) What is the range of R ?
- c) What is the height of R ?
- d) Calculate R^{-1} .